The Aggregate Expenditure Model

A Stylized Look at Business Cycle Dynamics

Outline

1. The Aggregate Expenditure Model

2. An Expanded Aggregate Expenditure Model

3. The Multiplier Effect

• Textbook Readings: Ch. 12

From Macro Variables to (Short-Run) Macro Models

- The first of three models The Aggregate Expenditure Model
 Solely output variables are in this model
- Next class: Aggregate Demand Aggregate Supply Model
 Both output and prices are in this model

Later: Expanded Loanable Funds Model (Monetary Policy)
 Output, prices and financial markets are in this model

A Quick Review

• We have **measurements**

GDP = C + I + G + NX

- Consumption: Households purchases of goods and services
- Investment: Housing, business investment in equipment, software, buildings plus inventories
- Government spending: defense, infrastructure, social security, ...
- Net exports: Exports minus imports

- We need a model
 - What forces drive the overall economy?

What Are We Looking For With This Model?

• We acknowledge that **boom/bust cycles** are **regular** occurrences

- Periodically, we see **big imbalances**
 - Millions want jobs, but can't find them → Unemployment jumps
 - Millions want to drive cars and trucks → Gasoline prices soar and inflation jumps

 We want a model that identifies equilibrium, BUT ALLOWS FOR IMBALANCES

The Aggregate Expenditure Model: A Very Simple Picture

• The future is uncertain, so expectations drive decision makers

• In the AE model:

When plans go awry, inventories are the buffer

Inventory swings explain periods in which production was too big or too small

Swings in inventories over time drive the economy back toward equilibrium

Four Key Considerations

• Expectations drive decisions amid uncertainty

• When expectations are misguided, imbalances arise

• Market forces then push the economy back toward equilibrium

• Thus, the AE model describes a self-correcting system

What Do We Assume Away?

- The AE model ignores inflation and financial markets
 - We don't allow for very weak demand to lower the overall level of prices
 - We don't allow interest rates, stock prices, or other Wall Street dynamics to operate on their own
- We assume that swings in the economy are completely captured by swings in output
- Key idea: In a year, the level of GDP is mainly *determined* by the level of aggregate expenditure
 - Contrast: What determines output in the long run?

Aggregate Expenditure and Output in the Short Run

- Aggregate expenditure is total amount of spending in an economy:
 - Consumption (C)
 - Planned investment (I^p)
 - Government purchases (G)
 - Net exports (NX)
- Actual Investment = *Planned* investment + *Unplanned* Investment
- Difference between actual investment and planned investment is unplanned investment (flow)
 - Inventories: Goods that have been produced but not yet sold (stock)

The Aggregate Expenditure Model

- AE model focuses on the short-run relationship between total spending and real GDP, assuming that the price level is constant
- Aggregate Expenditure:

$$AE = C + I^p + G + NX$$

• Remember:

GDP = C + I + G + NX

Macroeconomic Equilibrium:

AE = GDP

Let's Make the Model Simpler

Let's assume NO GOVERNMENT

- No government taxes
- No government spending
- Let's assume NO FOREIGN SECTOR
 - No exports
 - No imports

Then

AE = C + I

Interpretation

Y = C+I Income Aggregate Expenditure or or Output Aggregate Spending

GDP Identity vs. Equilibrium Condition

- **GDP identity**: $Y^a = C^a + I^a$
 - Y^a = Actual Real Income = Actual Real Output
 - C^a = Actual Real Consumption Expenditures
 - I^a = Actual Real Investment Expenditures

Always true when variables are actual magnitudes

GDP Identity vs. Equilibrium Condition

• Equilibrium condition: $Y^p = C^p + I^p$

Y^p = Planned Real Income = Planned Real Output

- C^p = Planned Real Consumption Expenditures
- I^p = Planned Real Investment Expenditures

Only true in equilibrium when variables are planned magnitudes

Assumptions

Y^a = Y^p = Y : Actual Income = Planned Income

C^a = C^p = C : Actual Consumption Expenditures = Planned Consumption Expenditures

|a = |p + |u|

- I^a: Actual Investment Expenditures
- I^p: Planned Investment Expenditures
- I^u: Unplanned Investment Expenditures

• Assume: $I^p = I \implies I^a = I^p + I^u = I + I^u$

• Note: Income equals expenditures

• In equilibrium, unintended inventory expenditures equal zero

GDP Identity: $Y = C + I^a = C + I + I^u$

Equilibrium Condition:
$$Y = C + I$$

Production vs Expenditure: A Graphical Example



Slope?

The AE Model: The Graphical Backdrop

The Relationship between Planned Aggregate Expenditure and GDP on a 45 $^\circ\,$ -Line Diagram

- The X axis tracks output, Y
 - Since output equals income, the X axis also tracks income
- The Y axis tracks aggregate expenditure, AE

• Y = AE along the 45° line



Aggregate Expenditure(AE), Output(Y) and Employment

Macroeconomic Equilibrium

- The 45° line: AE = GDP
 - Inventories are unchanged
 - Macro equilibrium
- AE above 45° line: AE > GDP
 - Unplanned inventory fall
 - GDP and jobs increase in the <u>next</u> period

• AE **below** 45° line: **AE < GDP**

- Unplanned inventory rise
- GDP and jobs decrease in the <u>next</u> period



Adjustments to Macroeconomic Equilibrium

The Relationship between Aggregate Expenditure and GDP

IF	THEN	AND
Aggregate expenditure is <i>equal</i> to GDP	inventories are <i>unchanged</i>	the economy is in <i>macroeconomic equilibrium.</i>
Aggregate expenditure is less than GDP	inventories <i>rise</i>	GDP and employment <i>decrease.</i>
Aggregate expenditure is <i>greater</i> than GDP	inventories <i>fall</i>	GDP and employment <i>increase</i> .

The AE Model: An Equilibrium Seeking Framework

 In microeconomics, we saw shifts toward equilibrium in supply/demand charts

 AE model, with inventory swings, provide a storyline for a system that seeks equilibrium

- Note:
 - Wall Street can make recessions worse (r_g down but r_c up)
 - Forces that, at times, DON'T push us toward equilibrium
 - Adverse feedback loops

A Simple Model That Can Explain Recessions



What Drives AE Components?

• What key variables explain swings in

C = consumption

I = Investment

Key Drivers of Consumption

Current Disposable Income

• Expected Future Disposable Income

• Wealth

Interest Rates

Consumers' State of Confidence

Disposable Income

• Real Disposable Income:

$$Y_{dis} = Y - TX + TR$$

TX = Real Personal Taxes

TR = Real Transfer Payments

Consumption Function

Relationship between consumption spending and disposable income

$$C = C(Y_{dis}) = \overline{C} + bY_{dis}$$

- \overline{C} = Autonomous Real Consumption Expenditure
 - Determined by the "State of Consumer Confidence"
 C
- b = Slope of the consumption function
 - 0 < b < 1

Consumption Function

The Relationship between Consumption and Income, 1960–2008



Why Do Consumers Spend, Even When Income Is Zero?

- A consumer who loses her job and has no unemployment benefits has zero income
 - She will still likely buy food, heat/cool her abode
 - For a time—till her savings run out?—she will likely pay her rent/make her mortgage payment
- Thus **autonomous consumption**, \overline{C} , occurs even at zero income

 That explains why the consumption function, C, intersects with the Y axis above zero

Slope of the Consumption Function

 Marginal propensity to consume (MPC): Loosely, if you get one more dollar of income, how much more do you spend?

$$b = MPC = \frac{Change \ in \ Consumption}{Change \ in \ Disposable \ Income} = \frac{\Delta C}{\Delta Y_{dis}}$$

Δ Consumption = Δ Disposable Income × MPC

- Assumption: 0 < MPC < 1
 - $\hfill Over \ long \ periods: MPC \approx 0.9$

MPC + MPS = 1

- Marginal Propensity to Save (MPS): Loosely, if you get one more dollar of income, how much more do you save?
- 1970-2000: MPC = 96% & MPS = 4%

• 2000-2010: MPC = 86% & MPS = 14%

MPS: The objective is wealth accumulation
Rising asset prices lessen the need to save



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Revised Consumption Function

$$C = \overline{C} + bY$$



•0 < b < 1



Key Drivers of Consumption

- Shifts **along** the curve:
- Current Disposable Income

Shifts of the curve:

- Changes in MPC (slope):
 - Expected Future Disposable Income
 - Wealth
 - Interest Rates
- Changes in autonomous expenditures (intercept):
 - Consumers' State of Confidence

Consumer Spending Will Change...

- 1. A consequence of a change in **income**
 - This is a movement along the consumption function
- 2. A consequence of a change in **confidence**
 - Autonomous consumption changes as confidence changes
 - This shifts the intersection of the consumption function with the AE axis
 - The slope of the line, b, does <u>not</u> change
- 3. A consequence of a change in wealth or future income expectations or interest rates
 - MPC changes when one of these variables change
 - A change in b, the MPC, changes the slope of the consumption function
 - The intercept of the line does <u>not</u> change

Application

• In 2009, both autonomous consumption and the MPC fell

- Falling sentiment drove autonomous spending down
- Plunging wealth drove the MPC down


Application

• In 2009, **C** is **down**, despite **Y** being slightly **up**

• AE model depicts sharp fall in spending and limited income rise



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A Model: A Grand But Useful Simplification

• We strip away many important issues

• We find a streamlined picture of the world

 Despite the picture's simplicity, we learn important things about how the real economy works

• The 'art' is to choose which model to use

An Expanded AE Model

AE Model: The Complete Picture

- We began with a super simple model
 - No government, no foreign sector

$$G = EX = IM = 0$$

• We focused on the consumption function

We Can Build on Our Simple Model

Real aggregate expenditure, AE • We began with the (trillions of 2005 dollars) consumption function on \$14 the diagram Y = AE12 If there was no other 10 expenditures, 8 macroeconomic C 6 equilibrium would be where the consumption 4 Consumption function crossed the 45° 2 line

12

14

10

\$2

0

6

8

Real GDP, Y (trillions of 2005 dollars)

We Add the Additional Components of AE

• We assume the other components are **not affected by income**

They are predetermined

 Autonomous expenditure: An expenditure that does not depend on the level of GDP

Recall: Confidence about the future affects autonomous expenditure

Key Drivers of Planned Investment

• Expectations of Future Profitability

Interest Rate

Taxes

Cash Flow

Political Uncertainty

Key Drivers of Net Exports

• P^{US} relative to P^{ROW}

- If $\pi^{US} < \pi^{ROW}$, prices of U.S. products increase more slowly than prices of products of other countries \rightarrow NX will **rise**
- Growth rate of GDP^{US} relative to the growth rates of GDP^{ROW}
 - When incomes in the US rise faster than incomes in other countries → NX will fall
- Exchange rate between the dollar and other currencies
 - As the value of the U.S. dollar rises, the foreign currency price of U.S. products sold in other countries rises, and the dollar price of foreign products sold in the U.S. falls → NX will fall

We Now Can Identify Equilibrium for the Entire Economy

Macroeconomic Equilibrium on the 45°-Line Diagram

- Vertical shifts in real
 expenditure because their values do not depend on income
- We call the top-most line the aggregate expenditure function
- Macroeconomic equilibrium: Income equals expenditure, i.e. Y = C + I + G + NX



Adjustment to Macroeconomic Equilibrium

- Equilibrium occurs at \$10 trillion
- What if real GDP were \$8 trillion?
 - AE would be higher than GDP. Inventories would fall
 - This would signal firms to increase production, increasing GDP
- The reverse would occur if real GDP were above \$10 trillion



Exercise

• Find equilibrium GDP using the following macroeconomic model:

- C = 1000 + 0.75Y
- / = 500
- *G* = 600
- *NX* = -300
- Y = C + I + G + NX

Consumption function Investment function Government spending function Net export function Equilibrium condition

- a. 800
- b. 1,800
- c. 2,400
- d. 7,200

A Numerical Example of Macroeconomic Equilibrium

Macroeconomic Equilibrium

REAL GDP (Y)	CONSUMPTION (C)	PLANNED INVESTMENT (/)	GOVERNMENT PURCHASES (G)	NET EXPORTS (<i>NX</i>)	PLANNED AGGREGATE EXPENDITURE (<i>AE</i>)	UNPLANNED CHANGE IN INVENTORIES	REAL GDP WILL
\$8,000	\$6,200	\$1,500	\$1,500	- \$500	\$8,700	-\$700	increase
9,000	6,850	1,500	1,500	-500	9,350	-350	increase
10,000	7,500	1,500	1,500	-500	10,000	0	be in equilibrium
11,000	8,150	1,500	1,500	-500	10,650	+350	decrease
12,000	8,800	1,500	1,500	-500	11,300	+700	decrease

In Sum

Our AE model is expectations based

• A consumption function is the driver

• Unplanned inventory changes can create a boom/bust cycle

 Responses to inventory changes drive the economy back toward equilibrium

What the AE Model Lacks

- AE model focuses EXCLUSIVELY on real economy swings
- When aggregate expenditures are strong and inventories fall, businesses increase PRODUCTION and EMPLOYMENT
- What about when factories are operating at full capacity?
 - The model cannot account for inflationary swings
 - In the real world, sometimes strong growth leads to upward pressure on prices and wages
 - That is why the central bank sometimes steps on the gas and sometimes steps on the brake

Changes in Income and the Multiplier Process

AE Model: The Multiplier and the Multiplier Effect

- Autonomous expenditure does not depend on the level of GDP
- A change in autonomous spending clearly shifts output
- By how much?

• That is what we examine as we develop the multiplier analysis

Assumptions

To simplify analysis

- No Government: G = TX = TR = 0
- Closed Economy: EX = IM = 0

"Completely slack" economic conditions:

- Prices are "sticky": P = P̄ → So we don't see falling wages moving output costs down and employment up
- Unemployment and Excess Capacity: Y < Y^{Cap} → Ample resources so there is room to produce above identified equilibrium

Why Those Conditions?

• Why do we need 'slack'?

- Analysis focuses on the total rise for output that we will get from an initial increase in aggregate expenditures
- If all factories are operating all day, and everyone is working, the economy has no capacity to produce additional output

Why do we need sticky prices?

- In the AE model we assume that the economy responds to strength or weakness SOLELY by increasing or decreasing production
- In the real world, a surging economy can lift prices as well as production—and an economy in free fall likely witnesses falling prices

For An Economy that Is Closed and Has No Government

Model

$$Y = AE$$

$$AE = C + I$$

$$C = \overline{C} + bY$$

$$I = \overline{I}$$

$$AE = \overline{C} + \overline{I} + bY$$

- Assume: 0 < b < 1 that is 0 < MPC < 1
- Mathematical derivation: Equilibrium level of real income

Y = AE

Basic Diagram

- Closed economy with no government
- Autonomous C and I are not a function of Y
- $\overline{C} + \overline{I}$ identifies the intercept of the AE line
- MPC = b determines the slope of the AE line



What If Autonomous Investment Spending Increase?

• Assumption: Increase in the "State of Confidence" of business firms

• Why? We posit there is an improved outlook for the economy

• Effects: Firms increase autonomous investment spending

Investment Spending Increase

Define:

 \overline{I} = Original Level of Autonomous Investment Spending

 $\overline{\overline{I}}$ = New Level of Autonomous Investment Spending

$$\Delta \overline{I} = \overline{\overline{I}} - \overline{I} > 0$$

change in autonomous investment spending new level original level

What is the Effect on Y or GDP?

Effect of an Increase in \overline{I} on the Expenditure Schedule



Effect of $\Delta \overline{I}$ on the Equilibrium Level of Real Income



Implications

 Principle: Shifts in autonomous spending cause changes in real income and output in the same direction

• Why? Shifts in autonomous spending cause changes in aggregate planned spending in the same direction

Applications

Shifts in autonomous spending are one reason that changes in Y take place

 When Y changes, look for shifts in autonomous spending as a possible cause

The Multiplier Effect

- An increase in autonomous expenditure → AE line shifts upward
- Multiplier effect → Process by which real GDP increases by more than AE
- Multiplier → The increase in equilibrium real GDP divided by the increase in autonomous expenditure



Multiplier

• Observe from the diagram that $\Delta Y > \Delta \overline{I}$

 Why is the change in Income bigger than the change in Autonomous Investment Spending?

 Increases in autonomous Investment Spending give rise to increases in induced Consumption Spending

The Underlying Cause of the Multiplier Effect

- Autonomous increase in expenditure increases output
- Output equals income
- Some portion of income received (wages + profits) is spent → Induced Consumption
- How much?
 - By the marginal propensity to consume
- This spending raises output and income, which again raises spending... MORE Induced Consumption...

Multiplier Stages

$$E = C + I = \overline{C} + \overline{I} + bY$$

Autonomous Induced Spending Spending

Primary Stage: Effects of an Increase in Autonomous Spending $\uparrow \overline{I} \Rightarrow \uparrow Y$ Secondary Stage: Effects of the Induced Spending Increase $\uparrow Y \Rightarrow \uparrow C \Rightarrow \uparrow Y$

The Multiplier Effect in Action

• Assume **MPC = 0.75**

	ADDITIONAL AUTONOMOUS EXPENDITURE (INVESTMENT)	ADDITIONAL INDUCED EXPENDITURE (CONSUMPTION)	TOTAL ADDITIONAL EXPENDITURE = TOTAL ADDITIONAL GDP
ROUND 1	\$100 billion	\$0	\$100 billion
ROUND 2	0	75 billion	175 billion
ROUND 3	0	56 billion	231 billion
ROUND 4	0	42 billion	273 billion
ROUND 5	0	32 billion	305 billion
		: :	
ROUND 10	0	8 billion	377 billion
		· ·	· · · · · · · · · · · · · · · · · · ·
ROUND 15	0	2 billion	395 billion
		· · ·	
ROUND 19	0	1 billion	398 billion
-		· · ·	· · ·
n	0	0	\$400 billion

How We Add Up the Multiplier Effect?

This becomes the infinite sum:

Total change in GDP = $100 \text{ billion} + MPC \times 100 \text{ billion} + MPC^2 \times 100 \text{ billion} + MPC^3 \times 100 \text{ billion} + MPC^4 \times 100 \text{ billion} + \dots)$ Which we can rewrite as:

Total change in GDP = $100 \text{ billion} \times (1 + MPC + MPC^2 + MPC^3 + MPC^4 + ...)$

by factoring out the initial \$100 billion increase in investment.

The general formula for the multiplier is:

Multiplier = $\frac{\text{Change in equilibrium real GDP}}{\text{Change in autonomous expenditur e}} = \frac{1}{1 - MPC}$

What is the multiplier in the previous example?

Eventual Effect of the Multiplier

- We cannot say how long this adjustment to macroeconomic equilibrium will take
- But we can calculate the value of the multiplier, as the eventual change in real GDP divided by the change in autonomous expenditures:

$$\frac{\Delta Y}{\Delta I} = \frac{\text{Change in real GDP}}{\text{Change in investment spending}} = \frac{\$400 \text{ billion}}{\$100 \text{ billion}} = 4$$

 With a multiplier of 4, each \$1 increase in planned investment or any other autonomous expenditure, eventually increases
 equilibrium real GDP by \$4

MPC Determines the Multiplier

- Redo the analysis, with a surge in precautionary saving
 MPC falls to 0.5
- Assume \$100 billion rise in autonomous investment
 - Multiplier?
 - Increase in Y?

How does the increase in Y with MPC = 0.5 compare when MPC = 0.75?

MPC and the Multiplier: Examples

• If the MPC is 0.6, the multiplier is $\frac{\Delta Y}{\Delta I} = \frac{1}{1-0.6} = \frac{1}{0.4} = 2.5$

• If
$$\Delta I = 100$$
, then $\Delta Y = 100 * 2.5 = 250$

• If $\Delta I = -80$, then $\Delta Y = -80 * 2.5 = -200$

• If the MPC increases to 0.8, the multiplier is $\frac{\Delta Y}{\Delta I} = \frac{1}{1-0.8} = \frac{1}{0.2} = 5$

• If the MPC decreases to 0.5, the multiplier is $\frac{\Delta Y}{\Delta I} = \frac{1}{1-0.5} = \frac{1}{0.5} = 2$

Implications

 Principle: A change in Autonomous Spending has a "multiplier" effect on Real Income

- Observations:
 - Size of the multiplier depends on b, which is the MPC
 - Intuition: The larger is b, the greater is the induced consumption spending that takes place in the secondary stage
Summarizing the Multiplier Effect

- 1. The multiplier effect occurs either when autonomous expenditure increases or decreases
- 2. Because the multiplier is greater than 1 (why?), the economy is sensitive to changes in autonomous expenditure
- 3. The larger the MPC, the larger the value of the multiplier
- 4. The model **omits** some real-world complications
 - For example, in practice as real GDP changes, imports, inflation, interest rates, and income taxes will change
 - This generally means that the value we estimate for the multiplier, from the MPC, is too high. We will address some of these shortcomings later

The Multiplier in Reverse: Great Depression of the 1930s



2005 dollars)

YEAR	CONSUMPTION	INVESTMENT	NET EXPORTS	REAL GDP	UNEMPLOYMENT RATE
1929	\$737 billion	\$102 billion	-\$11 billion	\$977 billion	3.2%
1933	\$601 billion	\$19 billion	-\$12 billion	\$716 billion	24.9%

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What If the Government Uses Fiscal Policy?

- Why might policymakers use **fiscal stimulus**?
 - The AE model drives the economy to an equilibrium, but one that may leave some jobless (remember: sticky wages don't adjust quickly)
- How might policymakers change the equilibrium in this model?
 Policymakers decide upon the level for G AE = C + I + G

- Policymakers also decide upon the level for T → Disposable income
- What is the value of the fiscal multiplier?

"Size of the Multiplier" vs. "Supply Side" Effects

 For Keynesians the size of the multiplier is the flux capacitor for fiscal policy.

 For Classical Economists, supply side effects are the flux capacitor for fiscal policy

"Size of the Multiplier": Debate Is Furious

- Maybe the MPC is 0.5, not 0.75, for policy changes
 - An MPC of 0.5 gives a multiplier of 2 not 4
- What is the MPC for a one time tax cut?
 - If you think you only get one check, you may react differently, spending only a small portion of the funds
 - If the tax cut goes to Bill Gates, is he likely to spend as much of it as if it goes to a struggling family with 4 in college?

 If the government cuts taxes, we must think about how household 'expectations' change

Ricardian Equivalence

- Some Classical Economists argue that the multiplier is ZERO
 - "I can't spend this tax cut because I know they will raise my taxes later"
 - It has important implications
- How does Ricardian Equivalence square with the facts?
 - Poorly
 - Households may save some portion of the tax cut
 - But a multiplier of zero doesn't square with the facts

Fiscal Multiplier Amid the Great Recession

 In January 2009, economist Robert Barro argued fiscal multipliers in the US were essentially ZERO

 Christina Romer, Obama's CEA Chair, asserted that in 2010 economic slack suggested they were as high as 1.6

• Note: These numbers are nowhere near 4

Multiplier for A Change in Taxes

- Unlike I, G and NX, with T the initial change in expenditure is MPC * Δ T (instead of Δ I, Δ G or Δ NX)
- Thus, the overall effect on income of the change in T is

$$\Delta Y = -MPC * \Delta T * \frac{1}{1 - MPC}$$

• So the **multiplier for taxes** is

$$\frac{\Delta Y}{\Delta T} = \frac{-MPC}{1 - MPC}$$

• If MPC = 0.75, a change in T has a multiplier of 3 instead of 4

Recall the Paradox of Thrift

- Saving = Investment
- But if everyone tries to save more
 - Demand plunges
 - Slashed jobs = Sharp declines in income
 - Sharp fall for output and income so SAVING FALL
 - Investment fall
- As everyone tries to save more, saving actually goes down!
- That is Keynes's paradox of thrift

The Multiplier Effect: The Paradox of Thrift

- In discussing the AE model, Keynes argued that if many households decide at the same time to increase their saving, they may make themselves worse off by causing AE to fall, thereby pushing the economy into a recession
- Lower incomes in the recession might mean that total saving does not increase
 - Despite the attempts by many individuals to increase their own saving
- Keynes referred to this outcome as the paradox of thrift
 - What appears to be something favorable to the *long-run* performance of the economy might be counterproductive in the *short-run*